



LINEUP WITH MATH™

Math-Based Decisions in Air Traffic Control for Grades 5 - 9

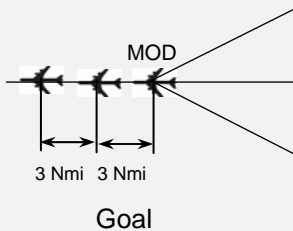
Problem Set C

Resolving 3-Plane Traffic Conflicts by Changing Route

Teacher Guide with Answer Sheets

Three planes on merging routes are:
-- different distances from the intersection,
-- traveling at the same speed.
An alternate route is available.

Overview of Problem Set C



Estimated class time: 1-1.5 hours

Objectives

In this Problem Set, students will determine whether three planes traveling on different merging routes will line up with proper spacing at MOD (the last intersection before the planes leave the airspace sector). If the spacing is not adequate, students will use alternate routes for one or more planes to achieve at least the proper spacing.

The planes are traveling at the same altitude and the same constant (fixed) speeds.

In *LineUp With Math™*, this is the first Problem Set to address three planes. Speed changes are not required to resolve spacing conflicts.

Each problem can be explored with the interactive Air Traffic Control (ATC) Simulator. Two of the problems can be more closely examined with Student Workbook C (print-based). The Workbook provides a structured learning environment for exploring the problems with paper-and-pencil worksheets that introduce students to pertinent air traffic control concepts as well as problem analysis and solution methods.

Prerequisites

Students will:

- Analyze a sector diagram to identify spacing conflicts among three planes, each traveling at the same speed.
- Resolve spacing conflicts by changing the route for one or more planes.

Before attempting the current Problem Set, it is *strongly* recommended that students complete Problem Set A that provides essential air traffic control vocabulary, units, and representations.

It is also recommended that students complete Problem Set B that introduces the ATC Simulator and enables students to explore the effects of a route change in a two-plane problem.



Materials

- ATC Simulator (web-based)
- Student Workbook C (print-based)

The materials are available on the *LineUp With Math™* website:

<http://www.smartskies.nasa.gov/lineup>

A separate student website gives students easy access to the Simulator only (and not to the answers and solutions provided on the teacher website):

<http://www.atcsim.nasa.gov>

ATC Simulator

A complete description of the ATC Simulator is contained in the Educator Guide for LineUp With Math™.

For a Simulator user guide and an animated tutorial, visit the LineUp With Math™ website.

Interactive Air Traffic Control Simulator

Students can explore Problem Set C with the interactive ATC Simulator. Each problem features a 3-plane conflict that can be resolved by a route change.

The Simulator problems for Problem Set C are:

3-1*; 3-2*; 3-7

Problems with an asterisk (*) are supported by worksheets in Student Workbook C.

For a complete set of answers and solutions to all Problem Set C Simulator problems, see Appendix I of this document.

For a discussion of the key points associated with the first two Simulator problems, see the worksheet notes in the following Student Workbook section.

Student Workbook

It is recommended that you have a copy of Workbook C open while you read these notes.

Each worksheet title is the same as the associated Simulator problem.

The Student Workbook consists of two worksheets, one for each of the two featured Simulator problems listed below.

<u>Simulator Problem</u>	<u>Worksheet Title</u>
3-1*	Problem 3-1
3-2*	Problem 3-2

Each problem features a spacing conflict with different starting conditions. As students progress through the worksheets, they likely will require less guidance and structure, and the subsequent worksheet reflects this.

For a complete set of answers to each worksheet, see Appendix II of this document.

For each worksheet, the key points are briefly described as follows.



*In the sector diagram, each route flows only **towards** MOD. E.g., a plane may fly from MINAH to OAL, but cannot fly from OAL to MINAH.*

Answer Sheets

For a set of answers and solutions to all Simulator problems, visit the LineUp With Math™ website.

Worksheet: Problem 3-1: Assure Spacing Among 3 Planes

- On a number line, students plot each plane's travel distance from MOD to help picture the arrival order of planes at MOD, their relative spacing, and any spacing violations,
- After students resolve a spacing violation with a route change, they again use a number line to picture the planes' new arrival order and spacing.

Worksheet: Problem 3-2: Assure Spacing Among 3 Planes

- This problem is similar to Problem 3-1. However, in this problem, students are expected to analyze and identify the conflict on their own. Minimal structure is provided to guide the students to a solution.

Answer sheets for each of the Problem Set C Simulator problems can be found in Appendix I of this document.

Answer sheets for each worksheet in Student Workbook C can be found in Appendix II of this document.



APPENDIX I

Air Traffic Control Simulator

Simulator Solutions for Problem Set C

3-1*, 3-2*, 3-7

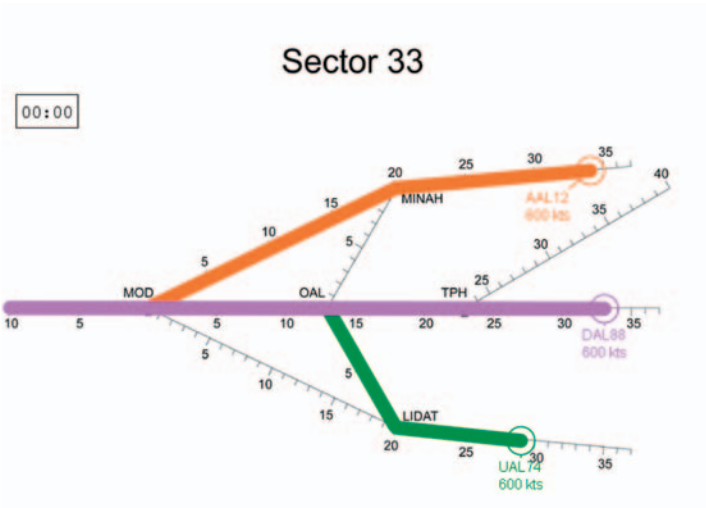
**Problems with an asterisk (*) are supported
by worksheets in Student Workbook C**



Problem 3-1

Solution

Starting Conditions:



Plane	From	Through	To	Distance	Speed
AAL12	MINAH		MOD	34	600
DAL88	TPH	OAL	MOD	33	600
UAL74	LIDAT	OAL	MOD	32	600

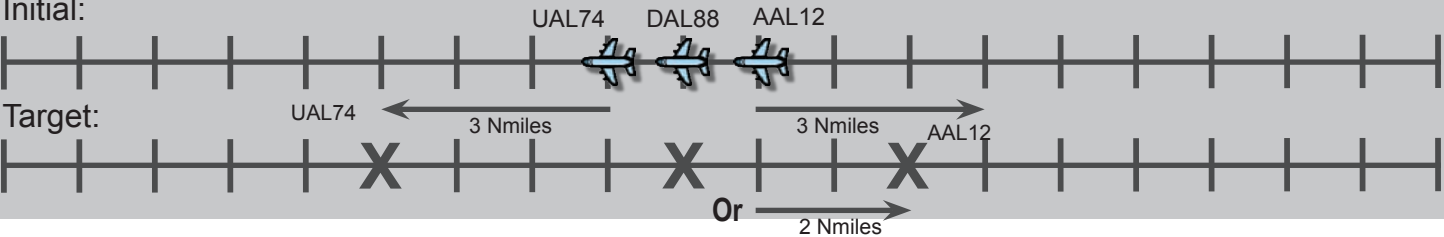
- Ideal spacing at **MOD** - 3 Nmiles

Analysis:

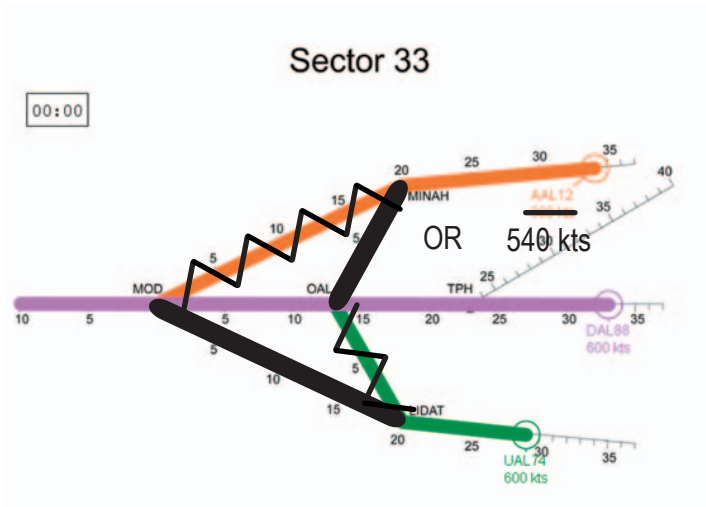
- **Conflict:** UAL74, DAL88 and AAL12 will arrive at MOD at each with 1 Nmiles separation.
- UAL74 can take the shortcut to shorten its travel distance.
- AAL12 can go through OAL to lengthen its travel distance by 3 Nmiles. (or slow down to fall back 2 Nmiles - best solution)

Projected Arrival	Plane	Distance Along Flight Plan	Initial Spacing
1st	UAL74	32	➤ 1 ➤ 1
2nd	DAL88	33	
3rd	AAL12	34	

Initial:



Solution:

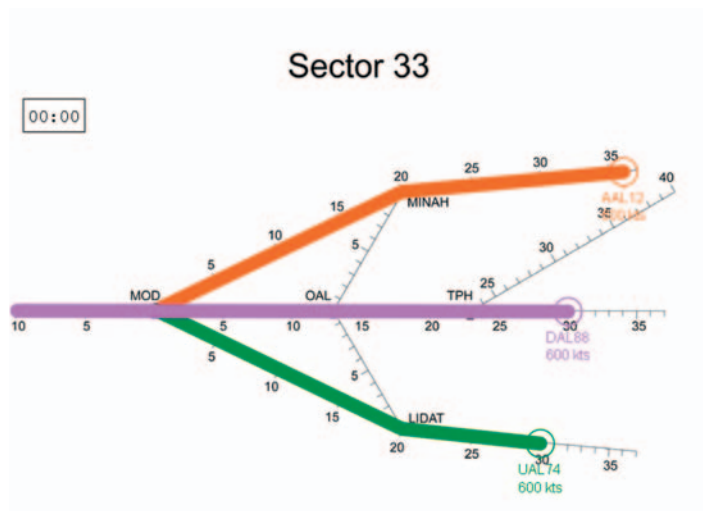


- UAL74 - Reroute direct MOD to move forward 3 Nmiles
- AAL12 - Reroute through OAL to fall back 3 Nmiles (Or, slow to 540 kts for 2 mins to fall back 2 Nmiles)
- Target Time - 3:42 mins. (route changes only)
- 3:36 mins. (route and speed change)

Problem 3-2

Solution

Starting Conditions:




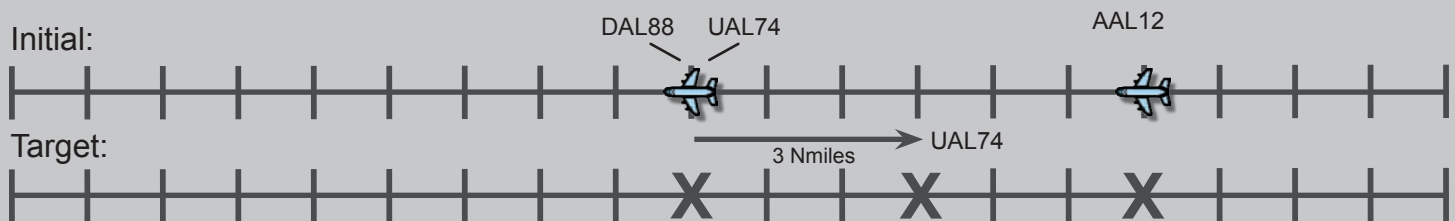
Plane	From	Through	To	Distance	Speed
AAL12	MINAH		MOD	36	600
DAL88	TPH	OAL	MOD	30	600
UAL74	LIDAT		MOD	30	600

- Ideal spacing at **MOD** - 3 Nmiles

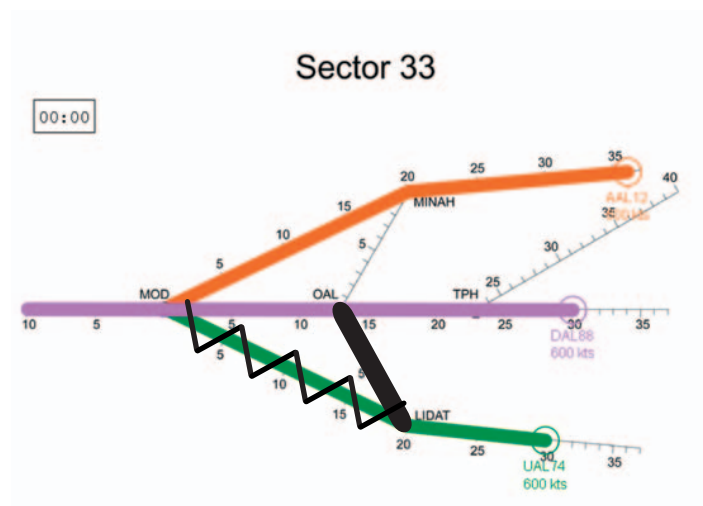
Analysis:

- **Conflict:** **UAL74** **AND** **DAL 88** will arrive at MOD at the same time.
- **AAL12** will be **6 Nmiles** behind.
- **UAL74** can go through OAL to lengthen its travel distance by 3 Nmiles.

Projected Arrival	Plane	Distance Along Flight Plan	Initial Spacing
1st	UAL74	30	
1st	DAL88	30	
2nd	AAL12	36	



Solution:



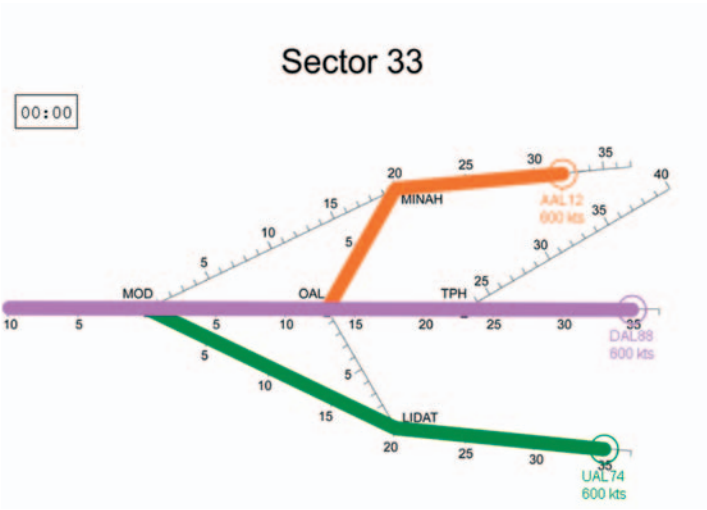
- **UAL74** - Reroute through OAL to fall back 3 Nmiles.
- **Target Time** - 3:36 mins.



Problem 3-7

Solution

Starting Conditions:




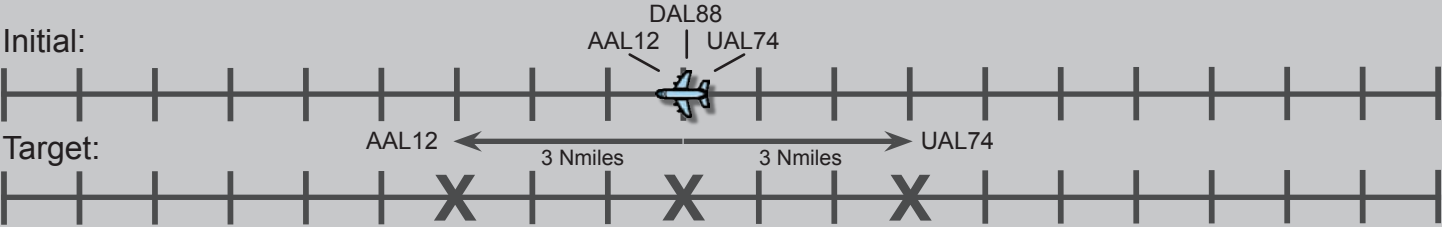
Plane	From	Through	To	Distance	Speed
AAL12	MINAH	OAL	MOD	35	600
DAL88	TPH	OAL	MOD	35	600
UAL74	LIDAT		MOD	35	600

- Ideal spacing at **MOD** - 3 Nmiles

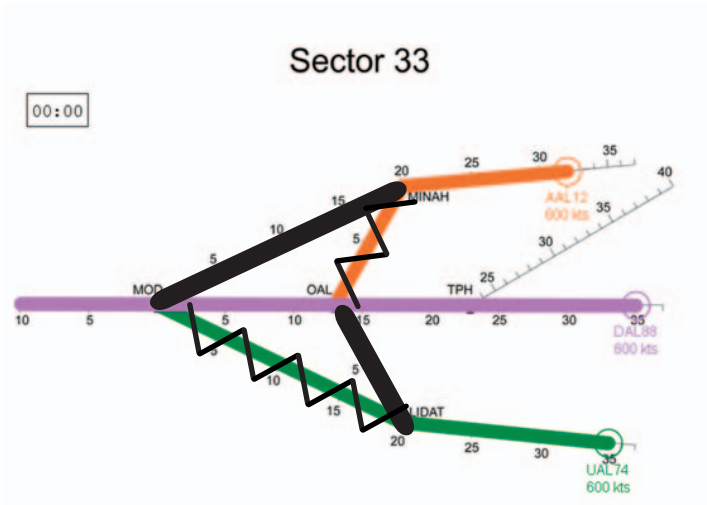
Analysis:

- **Conflict:** AAL12, UAL74, AND DAL 88 will arrive at MOD at the same time.
- **AAL12** can take the shortcut to shorten its travel distance by 3 Nmiles. **UAL74** can take the long route through OAL to increase its travel distance by 3 Nmiles.

Projected Arrival	Plane	Distance Along Flight Plan	Initial Spacing
1st	UAL74	35	
2nd	DAL88	35	
3rd	AAL12	35	



Solution:



- **AAL12** - Reroute direct to MOD to move forward 3 Nmiles.
- **UAL74** - Reroute through OAL to fall back 3 Nmiles.
- **Target Time** - 3:48 mins.



Math-Based Decisions in Air Traffic Control

Student Workbook C

Appendix II

- Resolving Air Traffic Conflicts by Changing Route
- 3 planes, each at the same speed
- Problems 3-1, 3-2

Workbook Answers



- Simulator at: www.atcsim.nasa.gov



United 74 cleared
Coaldale to Modesto.

Investigator: _____

An Airspace Systems
Program Product

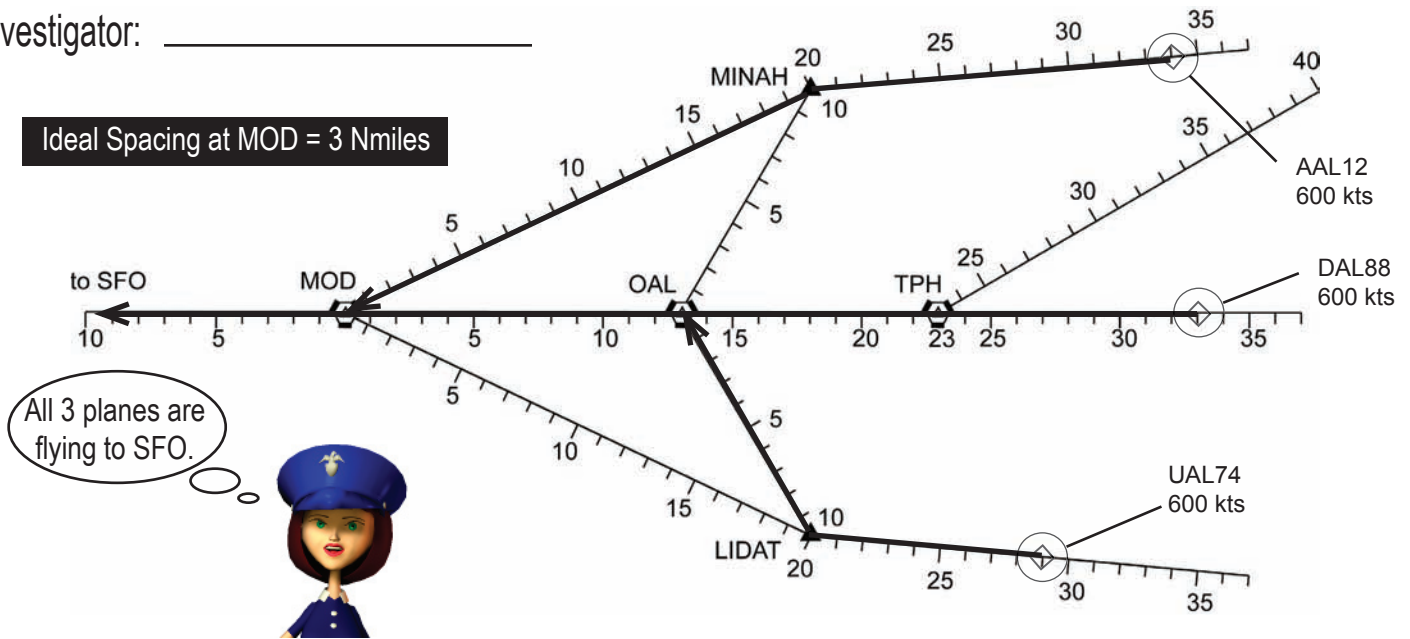



Problem 3-1



Investigator: _____

Ideal Spacing at MOD = 3 Nmiles



- Use the flight plans to find each plane's travel distance to MOD.
 - On the line below, use a  to plot the travel distance to MOD for each plane.
 - Label each plane.



- To fill in the table below:

 - Use your plot to figure out the arrival order and spacing at MOD.
 - See if any spacing is less than the minimum.
 - See if extra spacing is needed to get the Ideal Spacing.

Arrival Order at MOD:	1st	2nd	3rd
Plane Call Sign	UAL74	DAL88	AAL12
Spacing at MOD	1 Nmi	1 Nmi	
Is spacing at least the 2 Nmi minimum?	<input checked="" type="checkbox"/> No <input type="checkbox"/> Yes	<input checked="" type="checkbox"/> No <input type="checkbox"/> Yes	
Extra spacing needed for 3Nmi ideal	2 Nmi	2 Nmi	



3

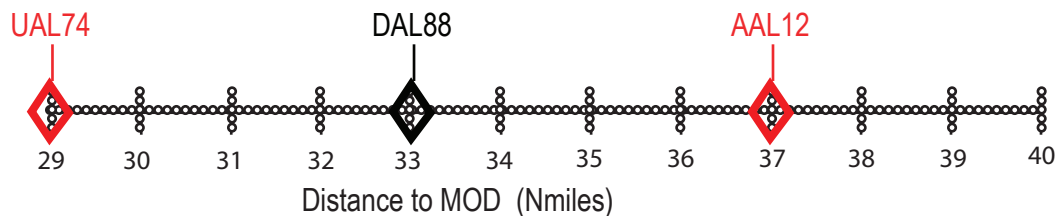
What route changes would you make to solve any spacing problems?

Arrival Order	Plane	New Route (if needed)	New Distance to MOD	New Spacing at MOD
1st	UAL74	LIDAT to MOD	29 Nmi	4 Nmi
2nd	DAL88		33 Nmi	4 Nmi
3rd	AAL12	MINAH to OAL to MOD	37 Nmi	4 Nmi

CAUTION: Be sure to mark out any old routes you've changed and darken the new routes.

4

To picture the NEW arrival order and spacing, use a  to plot the new distances to MOD for each plane on the line below. Label each plane.



5

With your new routes, are the spacings at least the Minimum Spacing (2 Nmiles)?

☐ No ☒ Yes

If No, try again.



6

With your new routes, are the spacings equal to the Ideal Spacing (3 Nmiles)?

☒ No ☐ Yes

7

If No, what could the controller do to make the spacing Ideal?

Change the speed of one or more planes.

End of Worksheet



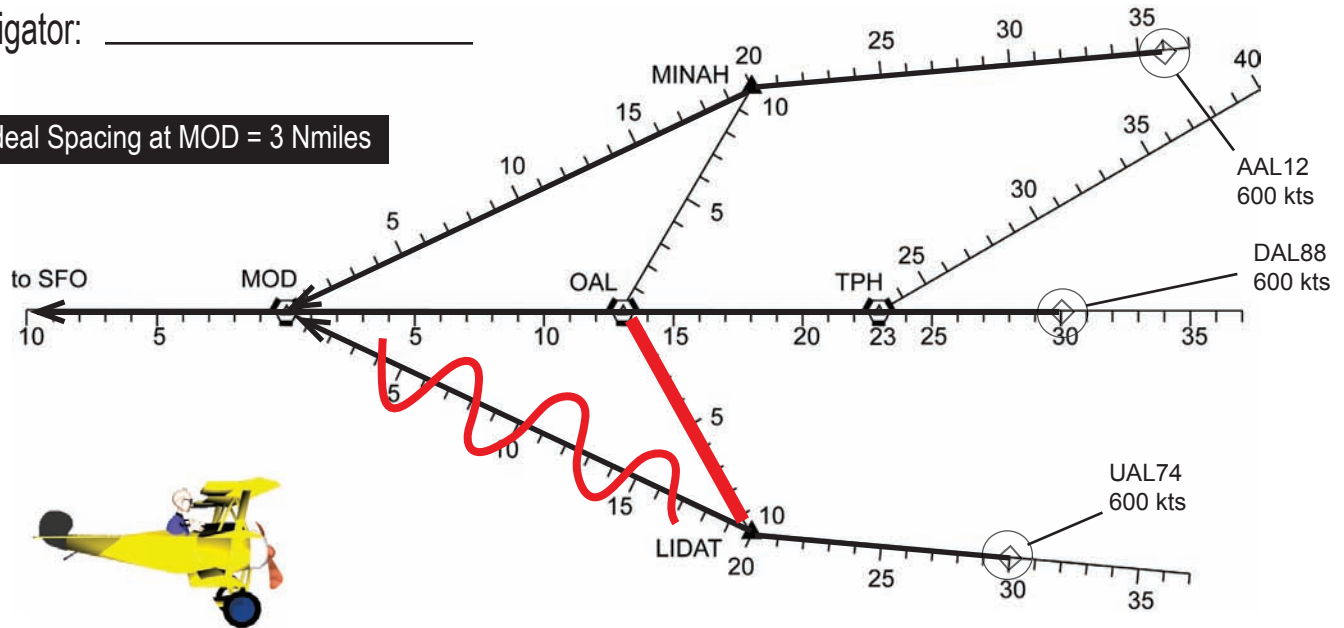


Problem 3-2



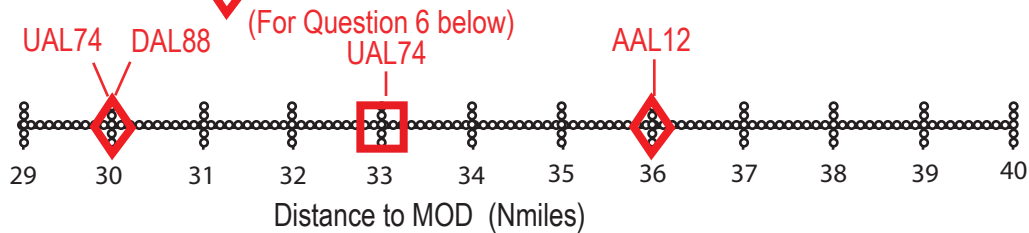
Investigator: _____

Ideal Spacing at MOD = 3 Nmiles



1

On the line below, use a  to plot the distance to MOD for each plane. Label each plane.



2

Are all the spacings at least the Minimum Separation? ☒ No ☐ Yes

3

Which plane needs extra spacing to have Ideal spacing? **UAL74** (There are no reroutes possible for DAL88.)

4


How much extra spacing is needed? **3** Nmiles

5

On the route diagram, show how you would reroute traffic to try to achieve the Ideal Spacing.

CAUTION: Be sure to mark out any old routes you've changed and darken the new routes.

6

On the line in Question 1, use a  to plot any NEW distances to MOD and cross out the old diamond for the old distance. Be sure to label each box with the plane's call sign.

7

Are all spacings now ideal? ☐ No ☒ Yes If Yes, Congratulations!

End of Worksheet

